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Amended Distance Bounds Using Eigenvalues of the Normalized Laplacian Matrix

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For a connected graph G, its normalized Laplacian matrix can be written as $\mathcal{L} = I - D^{\frac{-1}{2}}AD^{\frac{-1}{2}}$, where A is the (0,1) adjacency matrix and D is the diagonal matrix of vertex degrees. Suppose that X and Y are subsets of the vertex set of G. We consider two previously published upper bounds that relate the distance between X and Y to the eigenvalues of the normalized Laplacian matrix for G, the volumes of X and Y, and the volumes of their complements. We give a counterexample to both of the bounds, and then go on to provide corrected versions of each upper bound.