

*Fourth Seminar in Commutative Algebra and Related Topics,  
November 28-29, 2007, IPM, Tehran*

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Let  $(R, \mathfrak{m})$  be a  $d$ -

local

noetherian

ring

with

maximal

ideal

$\mathfrak{m}$

and

dimension

$d$ .

Let

$x_1, \dots, x_d$

be

parameters

of  $R$ .

Let

$R_t$

denote

the

local

noetherian

ring

$R_t$

with

maximal

ideal

$\mathfrak{m}_t$

and

dimension

$d$ .

Let

$\mathfrak{m}_t$

denote

the

local

noetherian

ring

$R_t$

$$x_1^t \dots x_d^t \notin (x_1^{t+1}, \dots, x_d^{t+1})R, \quad t \geq 0$$

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Let  $R$  be a local Gorenstein ring of dimension  $d$ . Let  $M$  be an  $R$ -module. Let  $\mathfrak{a}$  be an ideal of  $R$ . Let  $\mathfrak{m}$  be the maximal ideal of  $R$ . Let  $\mathfrak{p} \in \text{Supp}_R H_{\mathfrak{a}}^d(M)$ .

$$H_{\mathfrak{a}}^d(M) \simeq H_{\mathfrak{m}}^d(M) / \sum_{n \in \mathbb{N}} \langle \mathfrak{m} \rangle (H_{\mathfrak{m}}^d(M) \mathfrak{a}^n),$$

where  $\langle \mathfrak{m} \rangle A = \bigcap_{n \in \mathbb{N}} \mathfrak{m}^n A$ . Let  $\mathfrak{a} \subseteq R$ . Let  $H_{\mathfrak{a}}^d(M)$  be the  $\mathfrak{a}$ -th cohomology of  $M$ .

Let  $\mathfrak{m} \subseteq T$  be the maximal ideal of  $T$ . Let  $\mathfrak{m} \subseteq R$ .

$$\begin{aligned} & \left( H_{\mathfrak{a}}^d(M) \right) \\ & \left( H_{\mathfrak{m}}^d(M) \right) \sum_{n \in \mathbb{N}} \langle \mathfrak{m} \rangle (H_{\mathfrak{m}}^d(M) \mathfrak{a}^n) \\ & \left( H_{\mathfrak{m}}^d(M) \right) \sum_{l \in \mathbb{N}} \langle \mathfrak{m} \rangle (H_{\mathfrak{m}}^d(M) \mathfrak{a}^l) \subseteq \langle \mathfrak{m} \rangle (H_{\mathfrak{m}}^d(M) \mathfrak{a}^n). \end{aligned}$$

$$\begin{aligned} & \left( T/\mathfrak{a}T + \mathfrak{p} > 0 \right) \mathfrak{p} \in \text{Ass}_T(M \otimes_R T) \\ & \left( R(\mathfrak{a}, R/\mathfrak{p}) < d \right) \mathfrak{p} \in \text{Ass}_R M. \end{aligned}$$



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Let  $R$  be a local Noetherian ring,  $M$  a finitely generated  $R$ -module, and  $d$  a non-negative integer. Let  $C(\mathcal{D}(R), M)$  denote the set of all  $d$ -cocycles on  $R$  with values in  $M$ . Let  $H_m^d(M)$  denote the  $d$ -th local cohomology of  $M$  with respect to the maximal ideal  $\mathfrak{m}$ .

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Let  $\mathfrak{a}$  be a finitely generated  $R$ -submodule of  $M$  and  $N$  be an  $R$ -module. Then for any integer  $t \geq 0$ , we have

$$H_{\mathfrak{a}}^i(M, N) \cong \bigcup_{i \in \mathbb{N}} H_{\mathfrak{a}}^i(M/\mathfrak{a}^i M, N) \cap \{\mathfrak{p} \in \text{Spe } R \mid R/\mathfrak{p} \text{ is a local Artinian ring}\}$$

for all  $i < t$ . Moreover, we have

$$H_{\mathfrak{a}}^t(M, N) \cong \bigcup_{i \in \mathbb{N}} H_{\mathfrak{a}}^t(M/\mathfrak{a}^i M, N) \cap \{\mathfrak{p} \in \text{Spe } R \mid R/\mathfrak{p} \text{ is a local Artinian ring}\}$$

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## Some Results on Cofinite Modules and Local Cohomology

**A. R. Naghipour**

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Let  $R$  be a commutative Noetherian ring,  $\mathfrak{a} \subseteq \mathfrak{b}$  two ideals of  $R$  and  $M$  an  $\mathfrak{a}$ -cofinite  $R$ -module. For a non negative integer  $n$ , we prove that  $H_{\mathfrak{b}}^n(M)$  is  $\mathfrak{b}$ -cofinite whenever  $H_{\mathfrak{b}}^n(M)$  is Artinian and  $H_{\mathfrak{b}}^i(M)$  is  $\mathfrak{a}$ -cofinite for all  $i < n$ .

We generalized the Rees characterization of grade for  $\mathfrak{a}$ -cofinite modules and as a consequence, we extend the non-vanishing Grothendiecks Theorem and we shall show that the first non-vanishing local cohomology module  $H_{\mathfrak{c}}^t(M)$ , where  $\mathfrak{c}$  is an ideal of  $R$  such that  $\mathfrak{c}M \neq M$  and  $t = \text{grade}(\mathfrak{c}, M)$ , has only finitely many associated primes.

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## Cofinitenes of Local Cohomology Modules over Noetherian Rings

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Let  $R$  be a (not necessarily local) Noetherian ring and let  $M$  be a nonzero finitely generated  $R$ -module of finite dimension  $d$ . Let  $I$  be an ideal of  $R$  such that  $\dim R/I = 1$ . In this talk, the main result asserts that the local cohomology modules  $H_I^i(M)$  are  $I$ -cofinite; that is,  $\text{Ext}_R^j(R/I, (H_I^i(M)))$  is finitely generated for all  $i, j$ . Then the Bass numbers of  $H_I^i(M)$  are finite for all  $i$ . This generalizes the main results of Delfino-Marley [1], Yoshida [3] and [2, Main Theorem].

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## The Simplicial Join

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This is based on a joint work with M. Tousi and S. Yassemi.

Let  $\Delta$  and  $\Delta'$  be two simplicial complexes over two disjoint vertex sets. The simplicial join  $\Delta * \Delta'$  is defined to be the simplicial complex whose simplices are of the form  $\sigma \cup \sigma'$  where  $\sigma \in \Delta$  and  $\sigma' \in \Delta'$ . The aim of this talk is to study some algebraic and combinatorial properties of the simplicial join  $\Delta * \Delta'$  through the properties of  $\Delta$  and  $\Delta'$ .

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## Bounds on Regularity of Grade Modules with Local Base Ring of Dimension One

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Let  $M$  be a finitely generated graded module over a Noetherian homogeneous ring  $R$  with local base ring  $(R_0, \mathfrak{m}_0, k)$  where  $k$  denotes the residue field of  $R_0$ . In this talk we will show that the regularity of graded modules can be bounded in terms of some bounding functions where  $R_0$  is of dimension one. We will improve these bounds by setting some additional conditions on the local base ring  $R_0$ . The theme of this talk gives arise some questions on the regularity of graded modules when the local base ring  $R_0$  is of dimension two.