

ERRATA

Guillemin and Pollack, *Differential Topology*

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|-------|---------------|---|
| p. 5 | #4 | $ x < a$ |
| p. 6 | #8 | hyperboloid |
| p. 7 | #18b | $g(x) = f(x - a)f(b - x); h(x) = \frac{\int_{-\infty}^x g(t) dt}{\int_{-\infty}^{\infty} g(t) dt}$ |
| p. 12 | #8 | hyperboloid, and delete the parentheses |
| p. 16 | line 16 | in $f(X) \subset Y$ |
| p. 24 | line -11 | “In particular, taking X to be . . .” |
| p. 25 | #6 | This is the definition of homogeneity of degree m ; 0 is the only possible critical value |
| p. 27 | #11(a) | Remark: This is really a special case of Exercise <u>6</u> . |
| | #13 | Delete “of” at the end of the first line. |
| p. 28 | line 9 | $g \circ f : U \rightarrow \mathbf{R}^\ell$ |
| p. 45 | #6 | simply connected |
| p. 48 | #22 | $r_i = x - x_i $ |
| p. 51 | line -9 | $g(x, \frac{1}{t}v)$ |
| p. 52 | line -15 | exercise 15 |
| p. 55 | #11 | $f^{-1}(a)$ should be $\{x \in X : F(x, v) = a \text{ for some } v\}$. The HINT should read as follows. Show first that $F^{-1}(a)$ lies in a compact subset $\{(x, v) : v \leq \text{constant}\}$ of $T(X)$: for if $F(x_i, v_i) = a$ and $ v_i \rightarrow \infty$, pick a subsequence Now use the proof of the Stack of Records Theorem (p. 26, #7) to show that $F^{-1}(a)$ is indeed finite. |
| p. 56 | #15 | A and B are disjoint, closed subsets. |
| p. 61 | line 6 | $Z = \phi^{-1}(0)$ |
| | line -6,-5,-3 | dg_s and $d(\partial g)_s$ map to \mathbf{R}^ℓ |
| p. 62 | line 1 | $\ker dg_s$ has dimension $k - \ell$, $\ker d(\partial g)_s$ has dimension $k - \ell - 1$ |
| p. 64 | #10 | $df_z(\vec{n}(z)) < 0$ |
| p. 66 | #4 | $ x < a$ |
| p. 70 | line -10 | $S \rightarrow \mathbf{R}^M$ |
| p. 75 | #7 | affine subspace V ; the map given in the hint should be $\mathbf{R}^\ell \times S \times \mathbf{R}^N \rightarrow \mathbf{R}^N$, defined by $(t, v, a) \mapsto t \cdot v + a$ |
| | #9 | $f : \mathbf{R}^k \rightarrow \mathbf{R}$ |
| p. 76 | #18 | $X \subset T(X)$ refers to $X \times \{0\}$ |
| p. 83 | #5 | contractible; there still is a dimension 0 anomaly, so one should require $\dim X > 0$ |
| | #6 | contractible |
| p. 84 | #9 | $I_2(f, Z) = 0, p \notin f(X) \cup Z$ |
| p. 85 | #15 | closed manifold C |
| | #16 | Consider the submanifold $F^{-1}(\Delta)$ |
| | line -10 | Corollary to Exercises 18 and 19, obviously |

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| p. 90 | #9 | Not so fast! To apply Exercise 8, we must use the fact that X is a compact hypersurface to produce a ray intersecting X (and transversely). |
| | #10 | small neighborhood of $-z/ z $. |
| p. 91 | #11 | \overline{D}_1 is compact; “parametrization” in last line. |
| p. 99 | line 8 | sign |
| p. 106 | #18 | (b) nonzero normal vectors |
| | #21 | What does it mean to define a manifold with boundary by independent functions? |
| | #23 | X orientable and connected |
| p. 117 | #9 | $g(t + 2\pi) = g(t) + 2\pi q$ |
| p. 131 | #4 | “is” stable |
| p. 136 | line 11 | The denominator should be $ \vec{v}(x) + tr(t, x) $ |
| p. 138 | #1 | $h_t(z) = e^t z$ |
| p. 139 | #7 | \vec{v}_1 should have only nondegenerate zeroes inside U |
| p. 140 | #12 | In the last formula, g^{ij} , not g_{ij} , where $(g^{ij}) = (g_{ij})^{-1}$ |
| | #14a | the matrix (g^{ij}) is nonsingular |
| p. 141 | #17 | sum of the indices of f at its critical points |
| p. 144-5 | #3 | The new map will only agree with f on the complement of a slightly larger ball, so it’s not quite an extension |
| p. 147 | #3 | $f(tx) = g_t(x)$ |
| | #6 | Replace ρ with β , b with a in the last three lines |
| | #8 | “Now apply the corollary of the special case” should be after the right parenthesis |
| p. 148 | #11 | ρ is not a submersion, but the rest is right |
| p. 155 | line 17 | $(T^\pi)^\sigma = T^{\sigma \circ \pi}$ |
| p. 164 | line -10 | $df_I = df_{i_1} \wedge \cdots \wedge df_{i_p}$ |
| p. 166 | line -3 | X is a k -dimensional oriented manifold with boundary |
| p. 170 | line 2 | $f_1 \circ h, f_2 \circ h, f_3 \circ h$ |
| | line 8 | $\vec{F} = (f_1, f_2, f_3) \circ h$ |
| p. 173 | #9 | The reference should be to Exercise 7 |
| p. 174-5 | | 1, 2, 3 magically become (a), (b), (c) |
| p. 187 | #11 | The reference should be to Exercise 12 |
| | #13 | We need Z_0 and Z_1 oriented, and the definition of cobordism needs to be updated to $\partial W = -Z_0 \times \{0\} \cup Z_1 \times \{1\}$. |
| p. 188 | line 5 | Y should be connected (cf. the proof on p. 191) |
| p. 190 | | In the lemma, X, Y should be compact, and \int_S should be \int_X ; in the proof, U should be a connected neighborhood of y |
| p. 191 | #1 | $\frac{x}{x^2+y^2} dy$ |
| p. 194 | #7 | last line: Identify c . |
| p. 195 | line -18 | parallelepiped |
| p. 200 | #8 | Delete the $\frac{1}{2}$ before the Hessian matrix |