

# ALGEBRAIC PROPERTIES OF THE PATH IDEAL OF A GRAPH

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(JOINT WORK WITH DARIUSH KIANI)

ABSTRACT. Let  $k$  be a field and  $R = k[x_1, \dots, x_n]$ . Suppose that  $G$  is a directed graph with  $n$  vertices. Associated to  $G$  is a squarefree monomial ideal,  $I_t(G)$ , called the path ideal of  $G$  of length  $t$ , where  $2 \leq t \leq n$ . We are interested in studying some algebraic properties of  $I_t(G)$ , in which  $G$  is a tree. We showed that  $R/I_t(L_n)$  is Cohen-Macaulay if and only if  $t = n$  or  $n/2$ , where  $L_n$  is a line.